

04 Feb 2024 - DBMS-II - Week 05

→ Practice exercises

Algorithm for dependencies using functional dependencies

$$R = (A, B, C, D, E)$$

$$\text{with } F = \{ A \rightarrow B, BC \rightarrow D \}$$

$$\begin{array}{l} \xrightarrow{\text{F}^+ \text{ dep:}} \\ AC \rightarrow D \end{array}$$

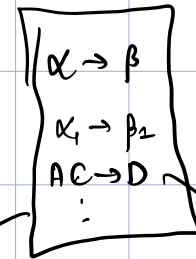
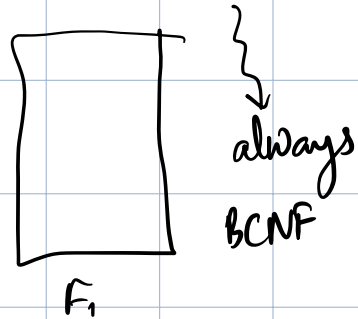
- decompose R into $R_1 = (A, B) \rightsquigarrow \text{BCNF} \checkmark$

- $R_2 = (A, C, D, E) \rightsquigarrow BC \rightarrow D \checkmark$

$$F^+ : \begin{array}{l} A \rightarrow B \\ BC \rightarrow D \\ AC \rightarrow D \end{array}$$

BCNF
↓
trivial/superkey

Decompose R into $R_1 = (A, B)$ and $R_2 = (A, C, D, E)$



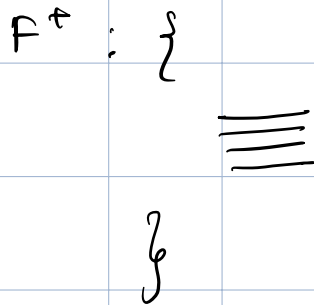
from R^+

check $\alpha \rightarrow \beta$

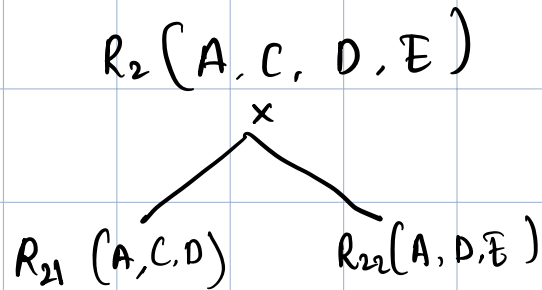
- ① trivial?
- ② α superkey?

If $AC \rightarrow DE$

not present, then not in BCNF.



$R_1(A, B)$
 ✓



Algorithm

result := {R} \ll set of all decompositions

\rightarrow see PDF bye :)

- lossless by not dependency preservation.
- exponential time complexity: finding already done relations in BCNF.
- You don't need to compute F^+ .

$A^+ \quad C^+ \quad D^+ \quad E^+$
 $AC^+ \quad CD^+$

} \rightarrow compute all
still exponential
but saves time.

→ BCNF is not dependency preserving. So check dependencies at run time since finding BCNF is expensive.

3NF decomposition algorithm

Example: $R = (A, B, C)$

$F = \left\{ \begin{array}{l} A \rightarrow BC \\ B \rightarrow C \\ A \rightarrow B \\ AB \rightarrow C \end{array} \right\}$

$F^c = \left\{ \begin{array}{l} A \rightarrow B \\ B \rightarrow C \end{array} \right\}$

$R_1 (BC)$

$R_2 (AB)$

Comparison of BCNF and 3NF

Design Goals

- 3NF decomposition
may not be
unique.
(different F_c)

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Multivalued Dependencies

→ One kind of redundancy that cannot be removed, even using BCNF.

→ inst_child (ID, child_name) ; inst_phone (ID, phone_no)
inst_info (ID, child_name, phone_no.)

→ an instructor can have multiple phone numbers and multiple children

}	9999	D	99341
	9999	W	94321
	9999	D	94321
	9999	W	99341

→ This relation is in BCNF

Multivalued dependency : definition

→ every functional dependency is a multivalued dependency.

$$\rightarrow \alpha \rightarrow \beta \Rightarrow \alpha \twoheadrightarrow \beta$$

$$\alpha \twoheadrightarrow \beta \Rightarrow \alpha \twoheadrightarrow R - \alpha - \beta$$

→ $D \rightsquigarrow$ set of multivalued and functional dependencies

→ $D^+ \rightsquigarrow$ closure

$\alpha \neq m \neq 2y$

Fourth Normal form

* $\alpha \twoheadrightarrow \beta$ is trivial ($\beta \subseteq \alpha$ or $\alpha \cup \beta = R$)
or α is a superkey

R_1 (ABCD)

$A \twoheadrightarrow BDG \cap R_1$

$A \twoheadrightarrow BD$

* $4NF \Rightarrow BCNF$

$R(A, B, C, G, H, I)$

$F = \left\{ \begin{array}{l} A \twoheadrightarrow B \\ B \twoheadrightarrow HI \\ CG \twoheadrightarrow H \end{array} \right\}$

→ not in 4NF : $A \twoheadrightarrow B$ and A is not a superkey.

a) $R_1 = (A, B) \rightarrow 4NF$

b) $R_2 = (A, C, G, H, I)$

→ R_2 is not in 4NF, decompose into R_3 & R_4 .

c) $R_3 = (C, G, H)$

d) $R_4 = (A, C, G, I)$

$A \twoheadrightarrow B \twoheadrightarrow HI$

$A \twoheadrightarrow I$

e) $R_5 = (A, I)$

f) $R_6 = (A, C, G)$

→ 8-8 Database Design Process