

R
(A, B, C, D, E)

set of functional dependencies F :
 $\alpha \rightarrow \beta$
 $\beta \rightarrow \gamma$

closure $F^+ = \begin{cases} \alpha \rightarrow \beta \\ \beta \rightarrow \gamma \\ \alpha \rightarrow \gamma \end{cases}$

F^+ check :

$\alpha \rightarrow \beta$ is trivial (i.e., $\beta \subseteq \alpha$)

α is a superkey for R

If a relation is in BCNF } chances of redundant info is very low

as per defn you have to find out F^+ but you don't need to

example:

not BCNF { in_dep (ID, name, salary, dept_name, building, budget)

α β

dept_name → building, budget

→ $\alpha \not\subseteq \beta$

→ α is not a superkey

∴ decompose

instructor (ID, name, salary, dept_name)

department (dept_name,
building,
budget)

Decomposing a schema into BCNF

→ Let $\alpha \rightarrow \beta$ be FD that causes violation of BCNF

decompose R into

$\alpha \cup \beta$: R_1 } $\rightarrow \alpha$, candidate key
 $R - (\beta - \alpha)$: R_2 } \rightarrow lossless

Is this decomposition lossless? What about dependency preservation?

in-dep (ID, name, salary, dept_name, building, budget)

α β
dept_name \rightarrow building, budget

R_1 : dept_name, building, budget

R_2 : ID, name, salary, dept_name

Example

$$R = (A, B, C)$$

$$F = \{ \underset{\textcircled{\checkmark}}{A \rightarrow B}, \underset{\textcircled{\times}}{B \rightarrow C} \} \quad \} \Rightarrow \begin{array}{l} A \rightarrow C \\ A \rightarrow BC \\ AB \rightarrow C \end{array}$$

$$R_1 := (A, B)$$

$$R_2 := (B, C)$$

$\therefore A$ is a candidate key

functional dependencies
MUST be satisfied
they come from the
business rules

to preserve dependency

Not always possible to

dept_advisor (s_ID, i_ID, dept_name)

violates BCNF
X

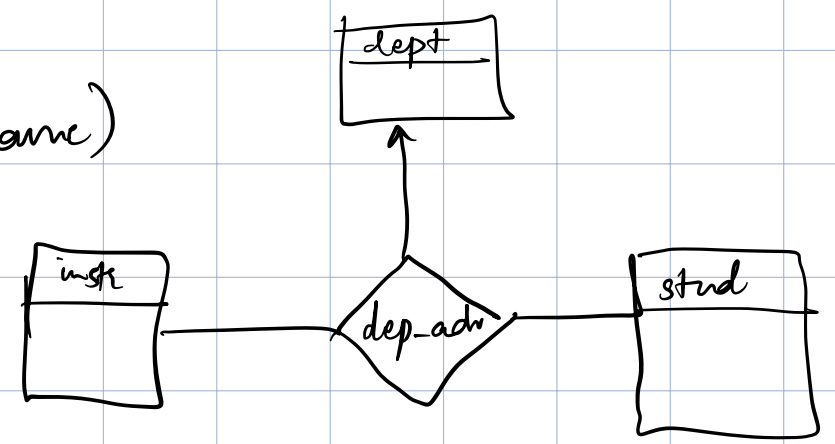
$i_ID \rightarrow dept_name$

$s_ID, dept_name \rightarrow i_ID$

not satisfying

$R_1 : i_ID, dept_name$

$R_2 : s_ID, dept_name$



each instructor can mentor only one student from a department

Third Normal Form

- guaranteed to preserve dependency
- some redundancy